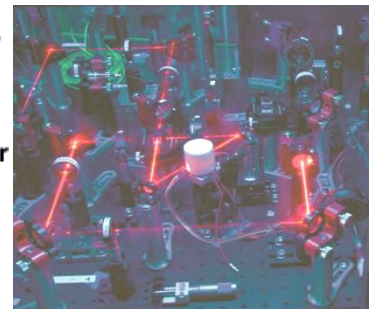
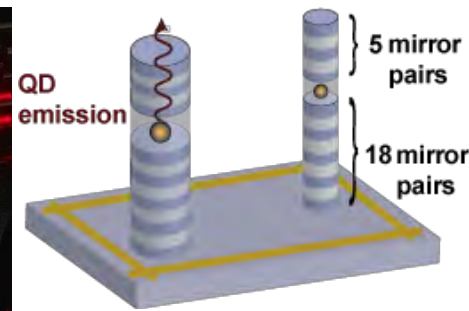
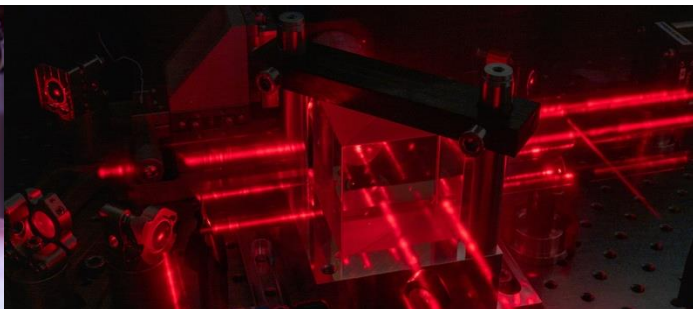
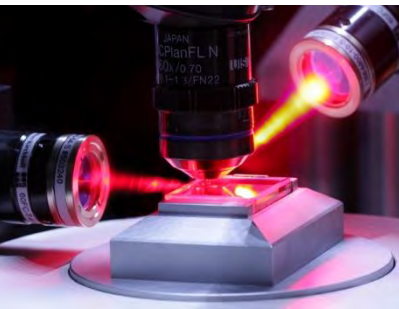
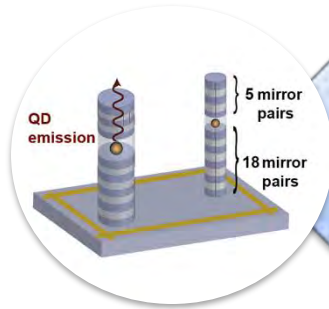


Quantum light from quantum emitters: efficiency, characterization, and entanglement generation

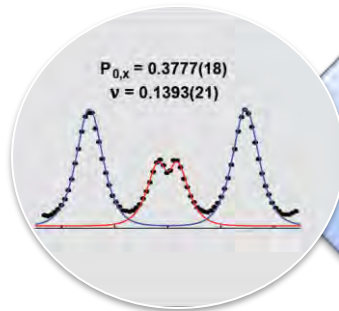
Ana Predojević
Stockholm University



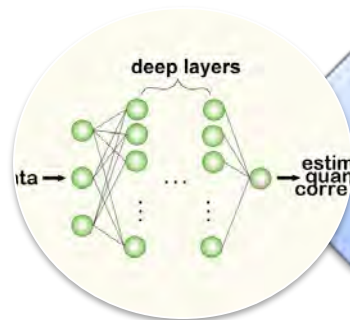
Quantum sources: efficiency, characterization, and entanglement generation



Novel sources of quantum light
Entanglement generation and efficiency engineering

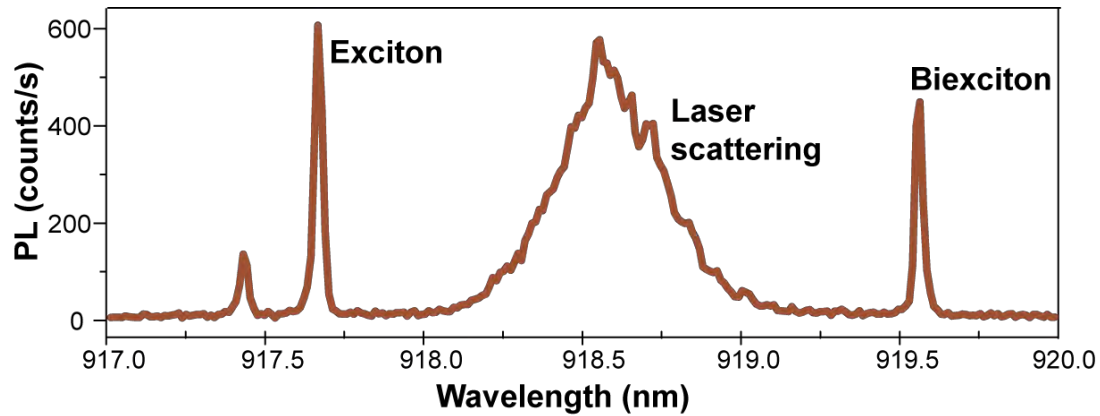


Intrinsic correlations
and two-photon interference and non-Gaussianity



Machine learning for quantum technologies
Entanglement quantification

Increasing the extraction efficiency



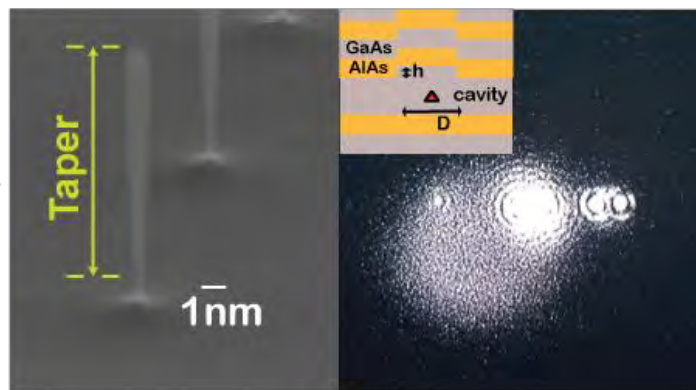
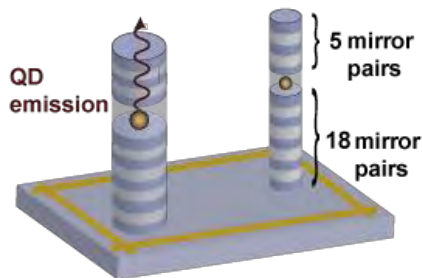
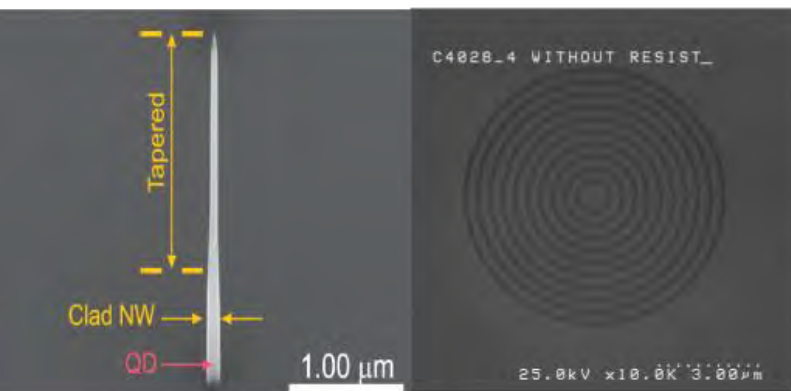
L. Ginés, et al. *Opt. Express* **29**, 4174 (2021).

J. Jurkat et al. *Phys. Rev. Materials* **5**, 064603 (2021).

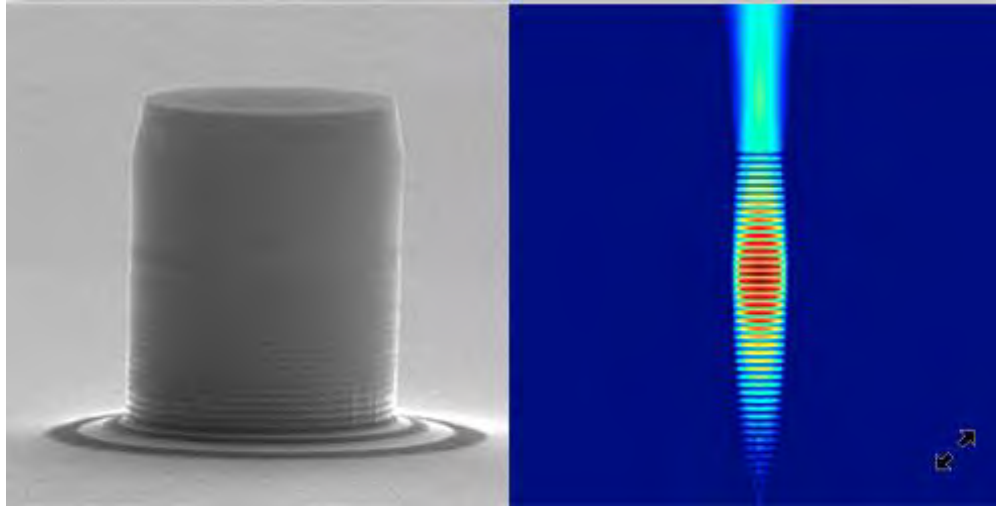
L. Ginés, et al. *Phys. Rev. Lett.* **129**, 033601 (2022).

T. Huber et al. *Nano Letters* **14**, 7107 (2014).

M. Khoshnegar et al. *Nature Comm.* **8**, 15716 (2017).



Increasing the extraction efficiency: low Q-factor cavity



Phys. Rev. Lett. 116, 020401(2016)

N. Somaschi, et al. Nature Photonics 10, 340–345 (2016)

X. Ding, et al. Phys. Rev. Lett. 116, 020401(2016)

S. Gerhardt, et al. Phys. Rev. B 100, 115305 (2019)

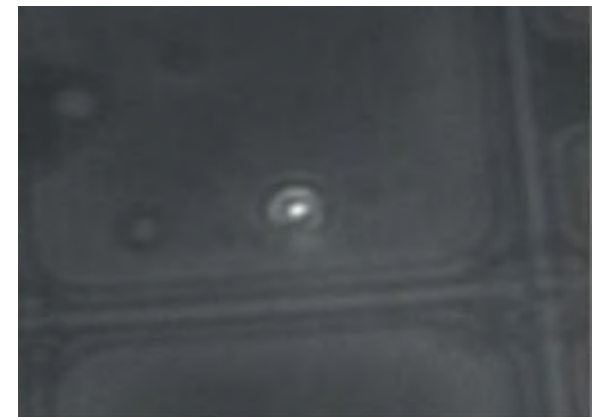
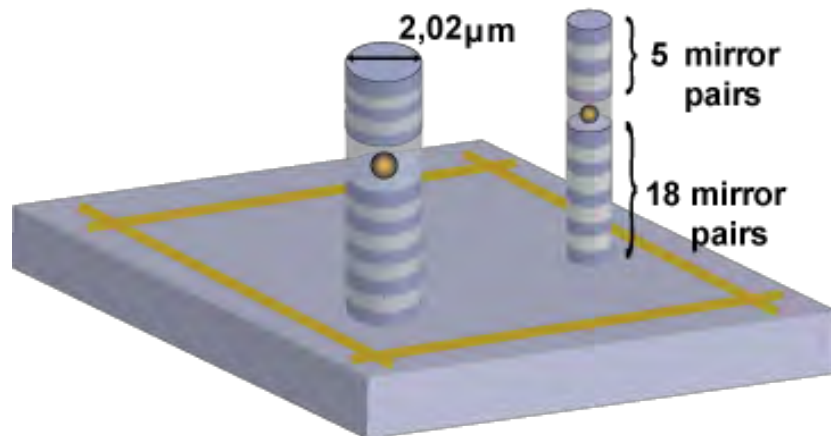
moderate to Q-factor: 1000 – 10000

linewidth < 0.5nm

Purcell factor up to 7

Increasing the extraction efficiency: low Q-factor cavity

$$\beta = \frac{F_p}{F_p + \Gamma_{supp}/\Gamma_{bulk}}$$



accuracy <30nm

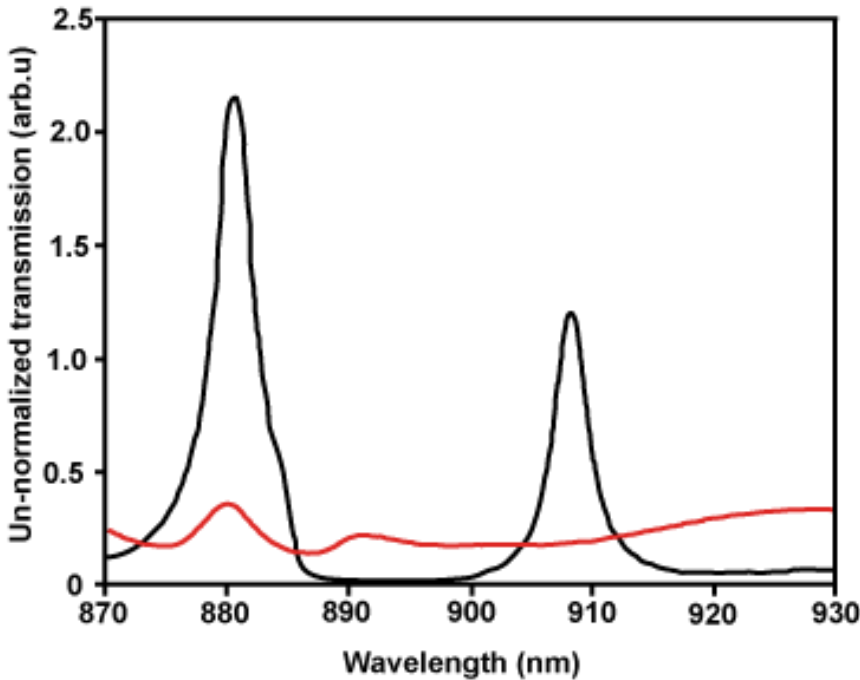
Low Q-factor design: 200-300

on average linewidth of 4.5nm FWHM

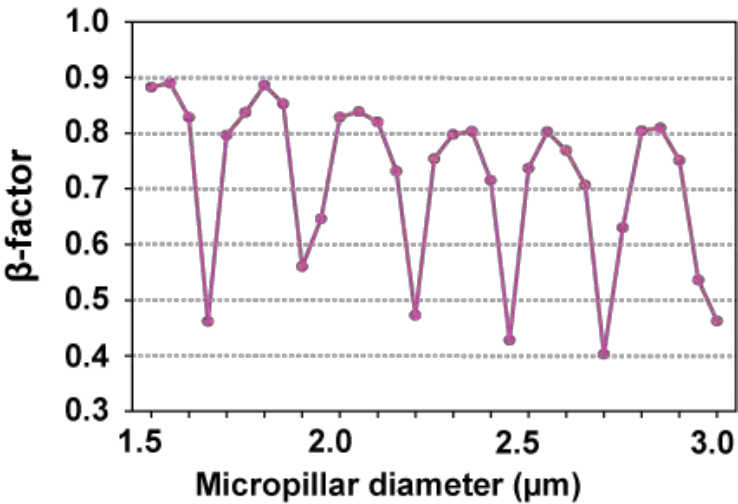
pillar diameter 1.6 – 8 μm

Increasing the extraction efficiency: low Q-factor cavity

1.50μm Pillar Diameter



$$\beta = \frac{F_p}{F_p + \Gamma_{supp}/\Gamma_{bulk}}$$



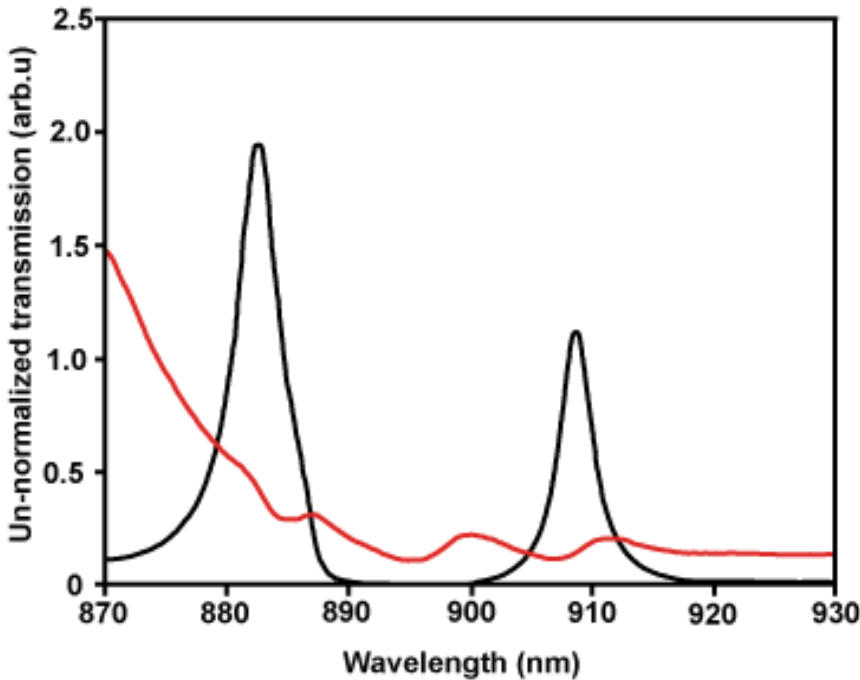
Low Q-factor design: 200-300

on average linewidth of 4.5nm FWHM

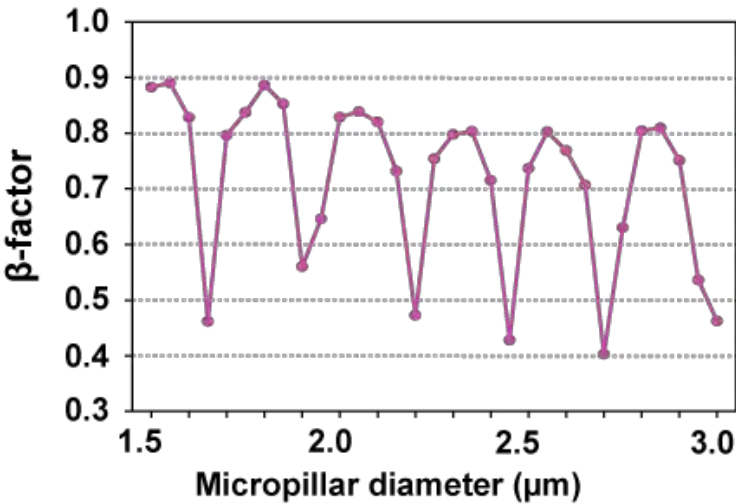
pillar diameter 1.6 – 8μm

Increasing the extraction efficiency: low Q-factor cavity

1.55μm Pillar Diameter



$$\beta = \frac{F_p}{F_p + \Gamma_{supp}/\Gamma_{bulk}}$$



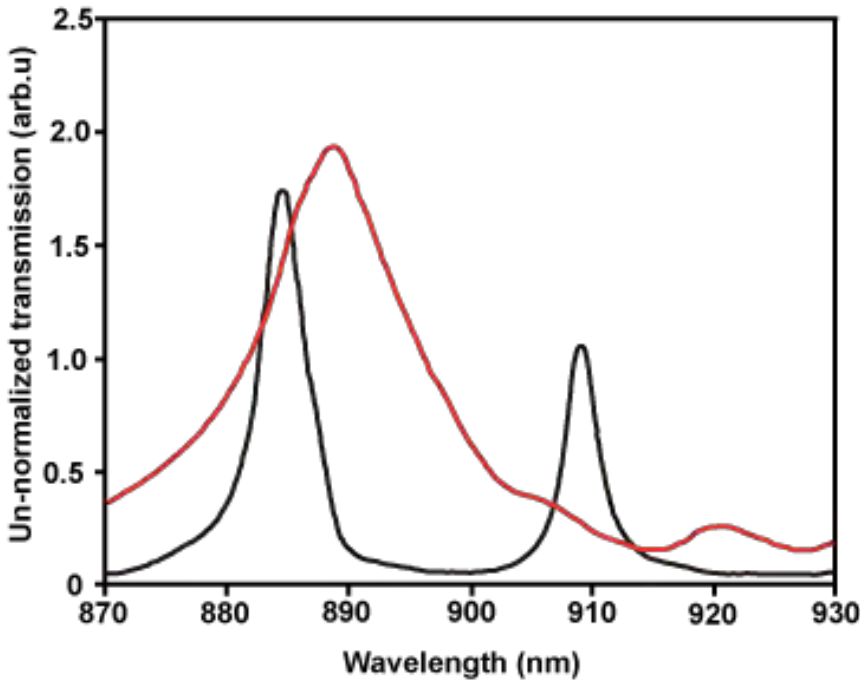
Low Q-factor design: 200-300

on average linewidth of 4.5nm FWHM

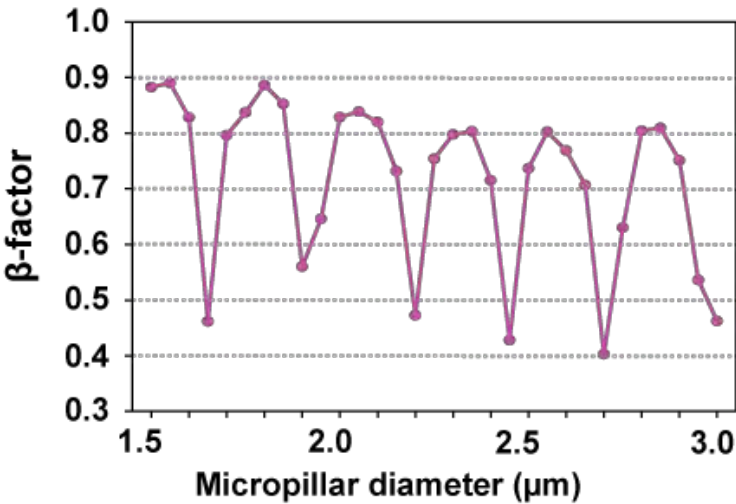
pillar diameter 1.6 – 8μm

Increasing the extraction efficiency: low Q-factor cavity

1.60μm Pillar Diameter



$$\beta = \frac{F_p}{F_p + \Gamma_{supp}/\Gamma_{bulk}}$$



Low Q-factor design: 200-300

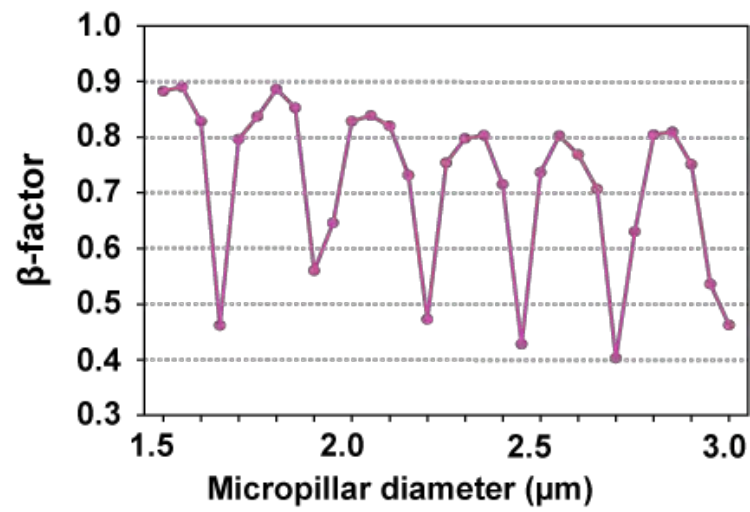
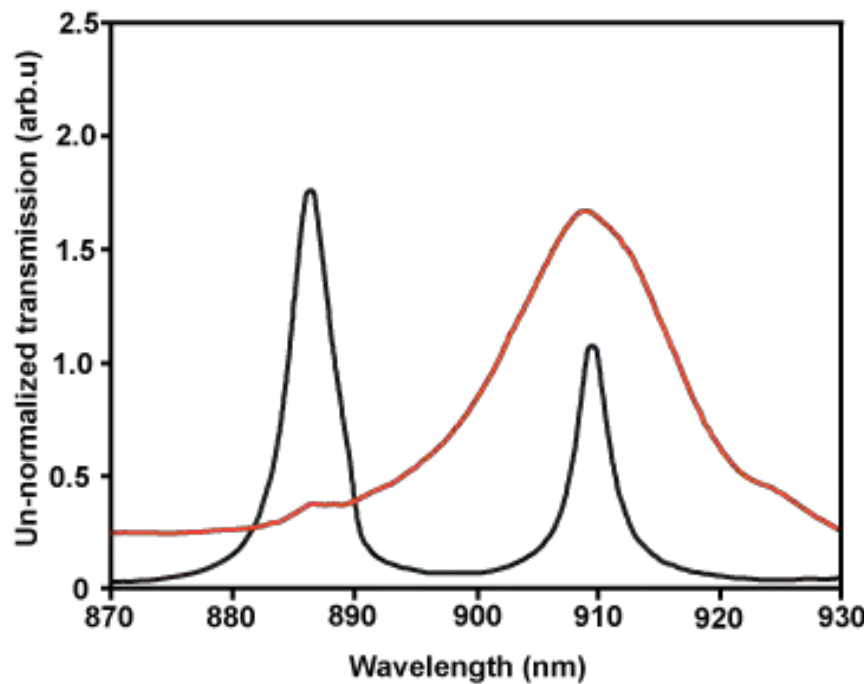
on average linewidth of 4.5nm FWHM

pillar diameter 1.6 – 8μm

Increasing the extraction efficiency: low Q-factor cavity

$$\beta = \frac{F_p}{F_p + \Gamma_{supp}/\Gamma_{bulk}}$$

1.65μm Pillar Diameter



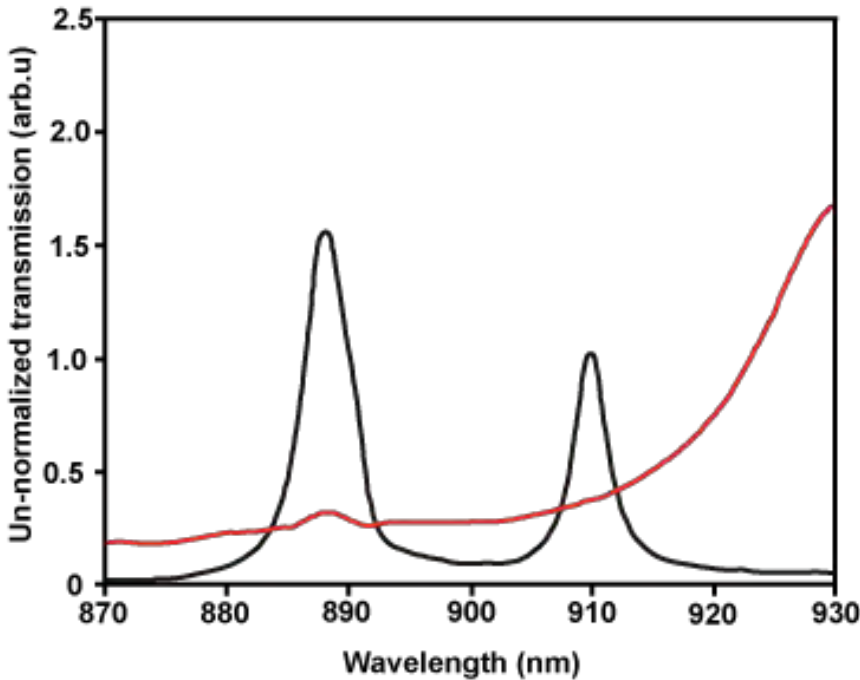
Low Q-factor design: 200-300

on average linewidth of 4.5nm FWHM

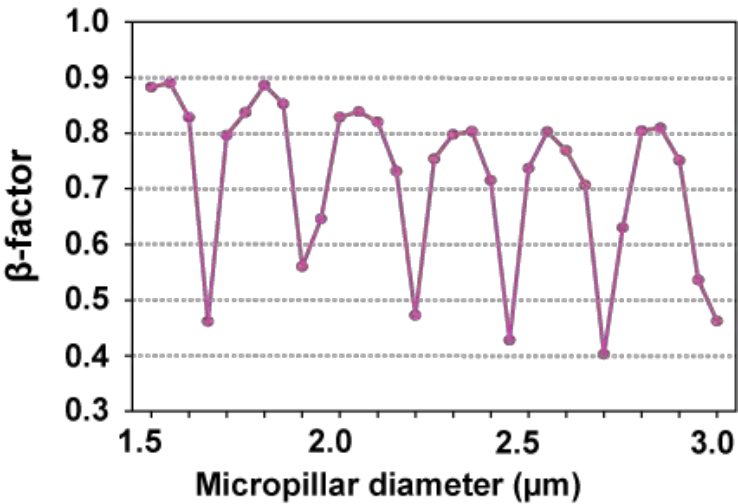
pillar diameter 1.6 – 8μm

Increasing the extraction efficiency: low Q-factor cavity

1.70μm Pillar Diameter



$$\beta = \frac{F_p}{F_p + \Gamma_{supp}/\Gamma_{bulk}}$$



Low Q-factor design: 200-300

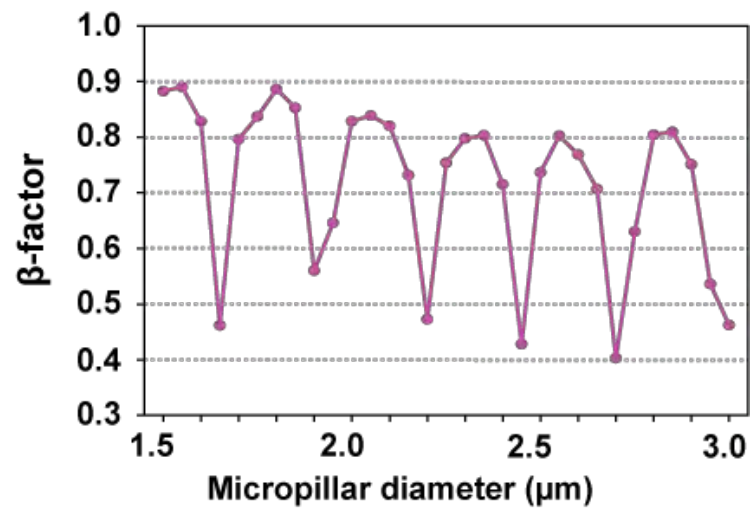
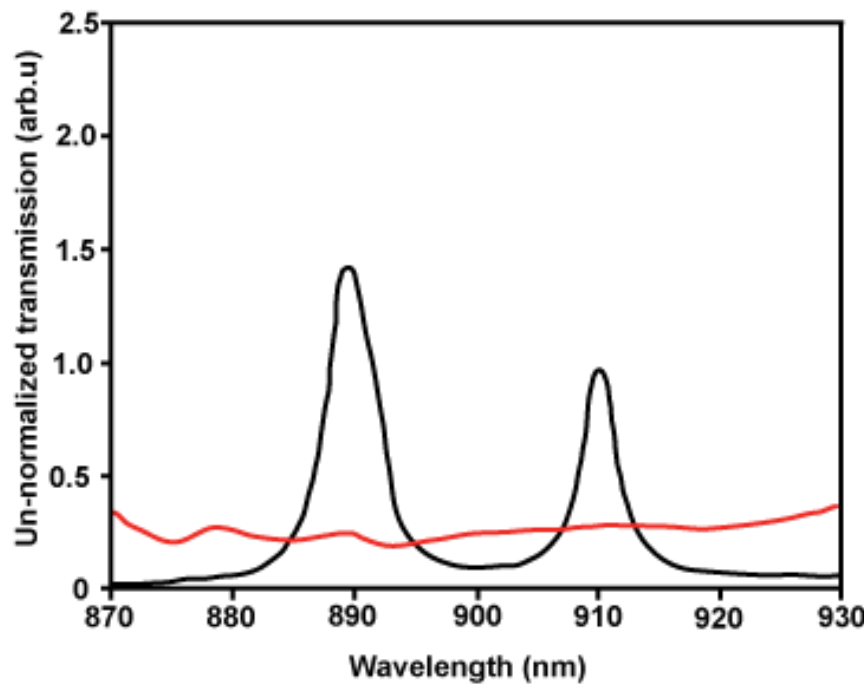
on average linewidth of 4.5nm FWHM

pillar diameter 1.6 – 8μm

Increasing the extraction efficiency: low Q-factor cavity

$$\beta = \frac{F_p}{F_p + \Gamma_{supp}/\Gamma_{bulk}}$$

1.75μm Pillar Diameter



Low Q-factor design: 200-300

on average linewidth of 4.5nm FWHM

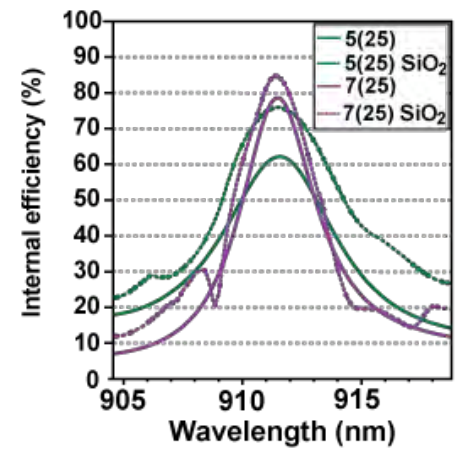
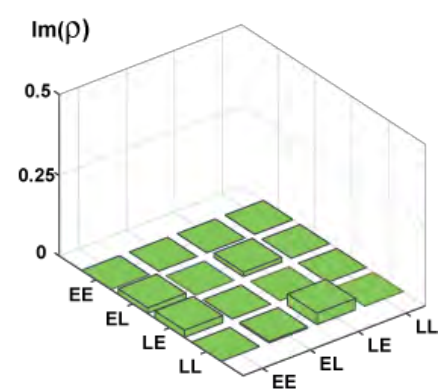
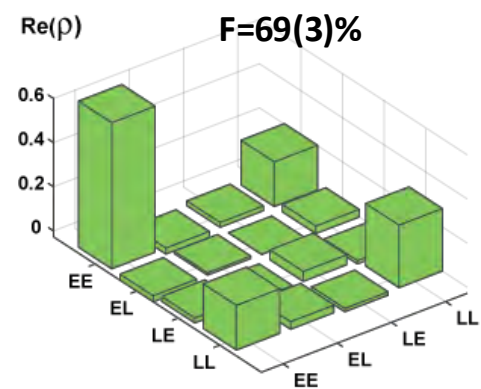
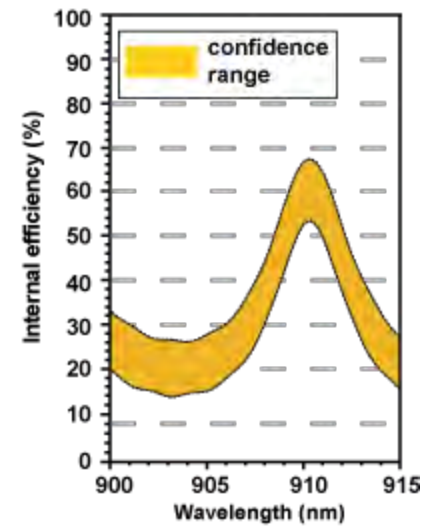
pillar diameter 1.6 – 8μm

Increasing the extraction efficiency: low Q-factor cavity

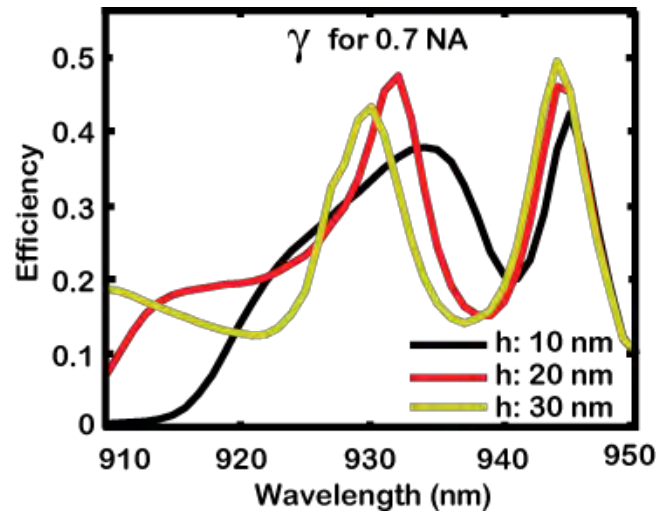
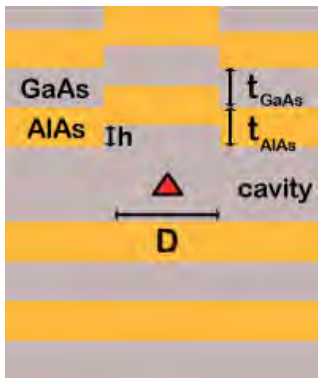
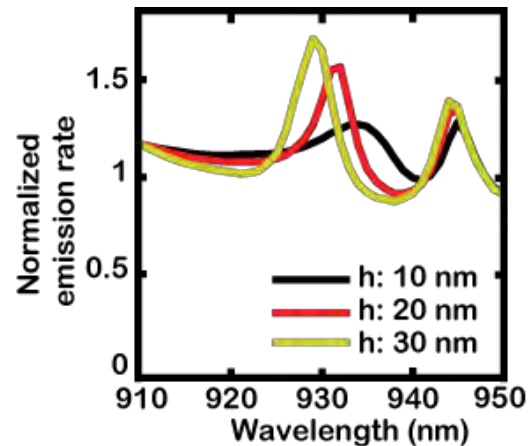
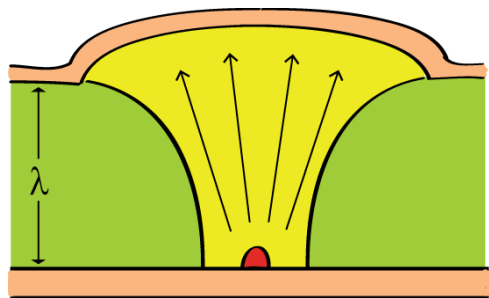
collection efficiency 69.4(10)% (0.68NA)

$$\frac{400(1)\text{kHz}}{\text{counts}}$$
$$\eta_{\text{det}} \times \eta_{\text{fc}} \times \eta_{\text{opt}} \times rr$$

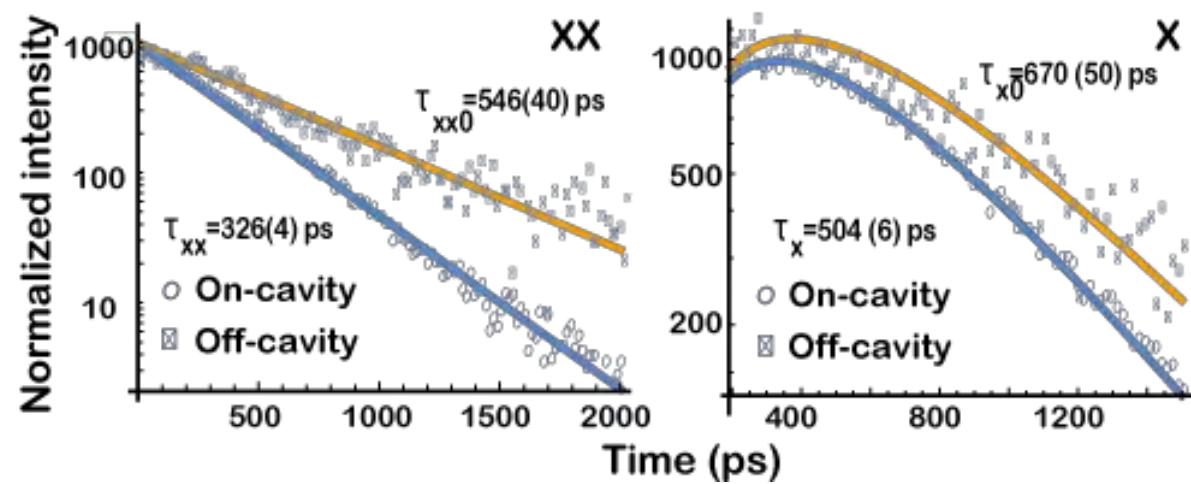
$0.40 \quad 0.29(1) \quad 0.06(1) \quad 80\text{MHz}$



Increasing the extraction efficiency: self-aligned cavity



Increasing the extraction efficiency: self-aligned cavity

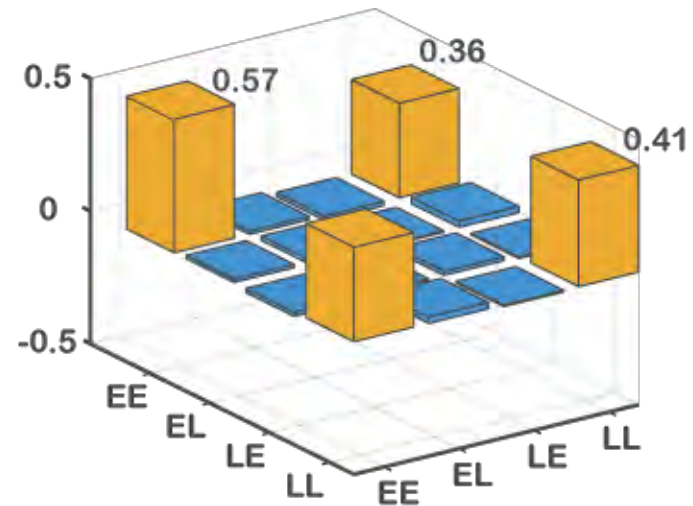
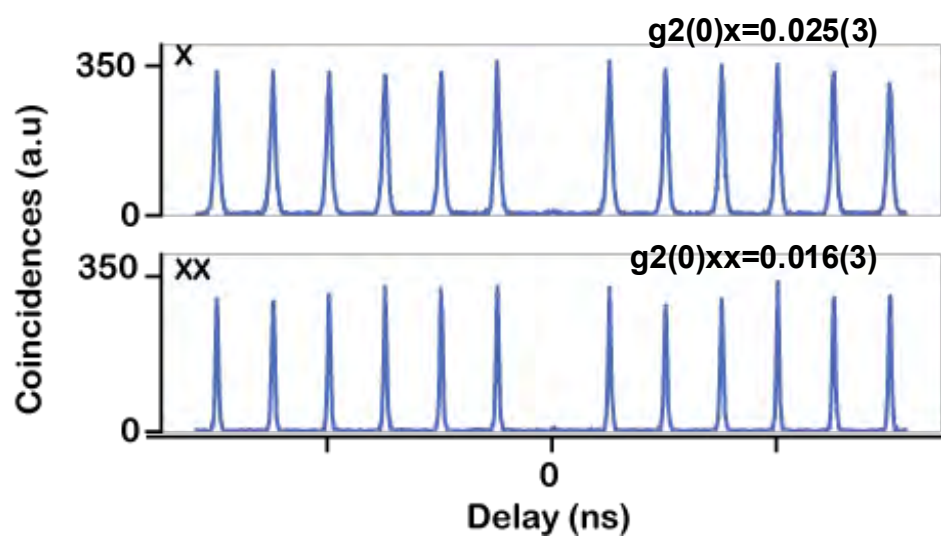


Purcell enhancement
(ranging from 1.2 to 1.7)

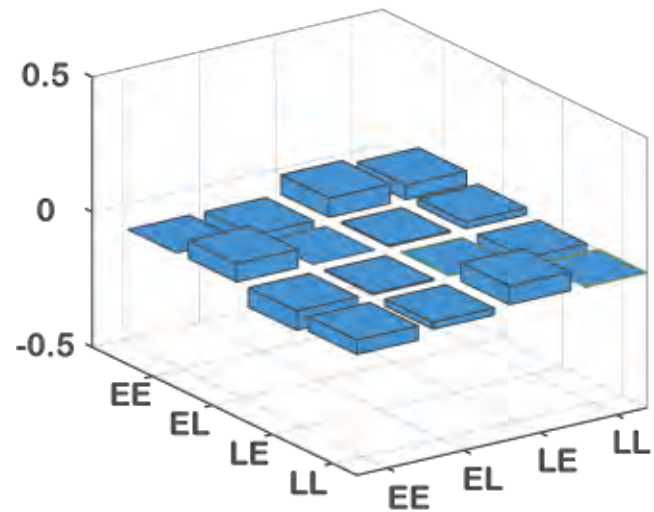
collection efficiency 17.1(10)% (0.62NA)



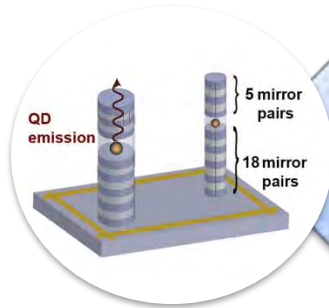
Increasing the extraction efficiency: self-aligned cavity



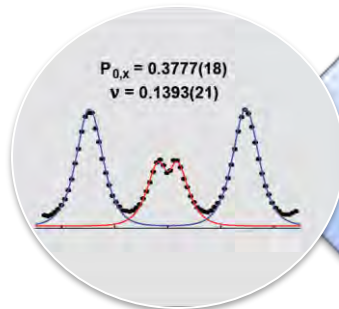
	time bin
concurrence	0.70 (10)
fidelity	0.84(4)



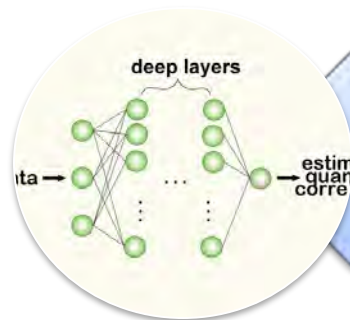
Quantum sources: efficiency, characterization, and entanglement generation



Novel sources of quantum light
Entanglement generation and efficiency engineering

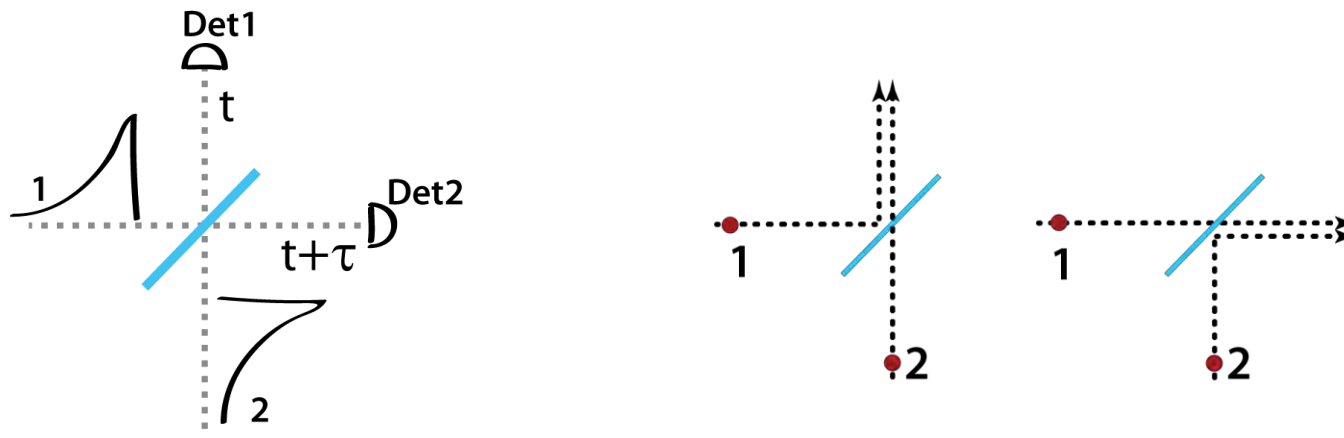


Intrinsic correlations
and two-photon interference and non-Gaussianity



Machine learning for quantum technologies
Entanglement quantification

Two – photon interference



$$G^{(2)}(t, \tau) = \frac{1}{4} [I_1(t) I_2(t+\tau) + I_2(t) I_1(t+\tau) - G_1^{(1)}(t, \tau) (G_2^{(1)}(t, \tau))^* - (G_1^{(1)}(t, \tau))^* G_2^{(1)}(t, \tau)]$$

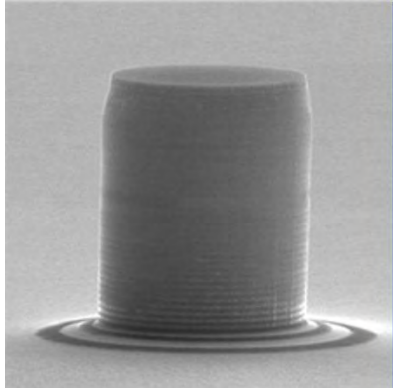
- in the case the photon 1 and photon 2 are identical

$$G^{(2)}(t, \tau) = \frac{1}{4} [2I(t)I(t+\tau) - 2|G^{(1)}(t, \tau)|^2]$$

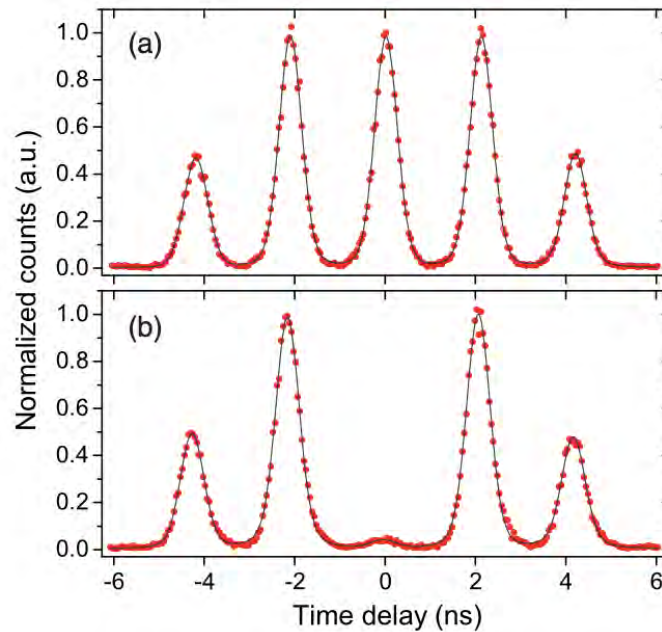
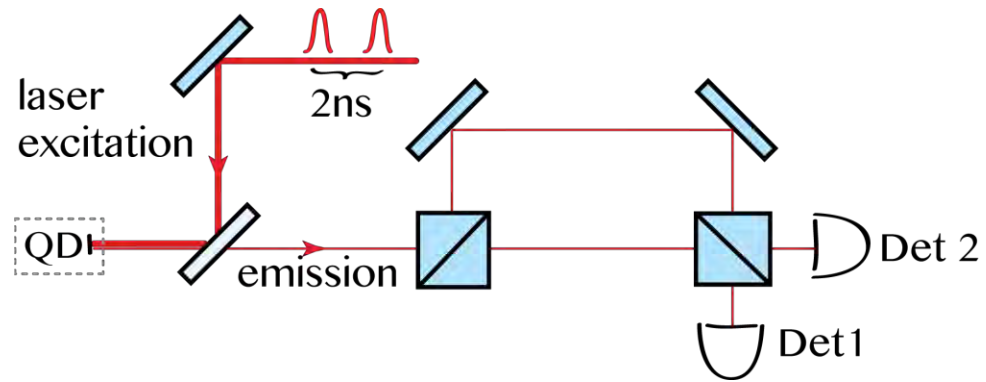
- importance of two-photon interference:

- quantum teleportation and entanglement swapping
- quantum photonic processors

Two – photon interference without cascade correlations



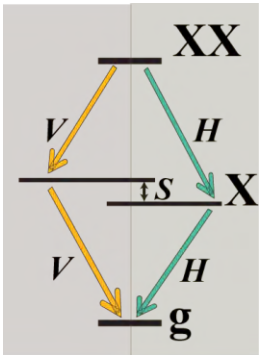
*Phys. Rev. Lett.*116, 020401(2016)



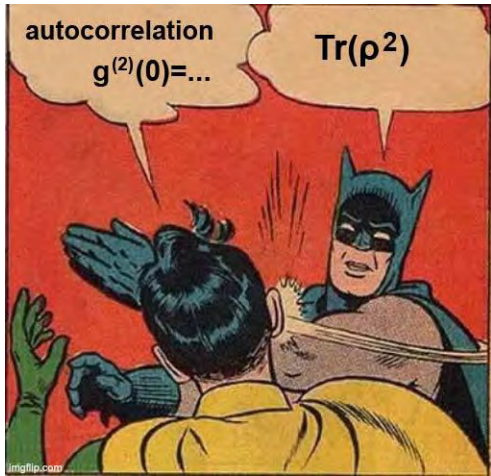
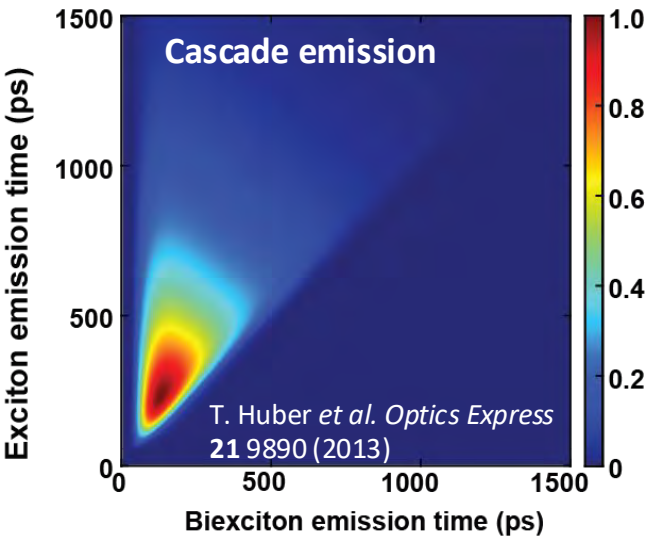
opposite polarizations
visibility= (max-min)/(max+min)= 1

equal polarizations

Cascade correlations



XX – Biexciton
X – Exciton
g – ground state

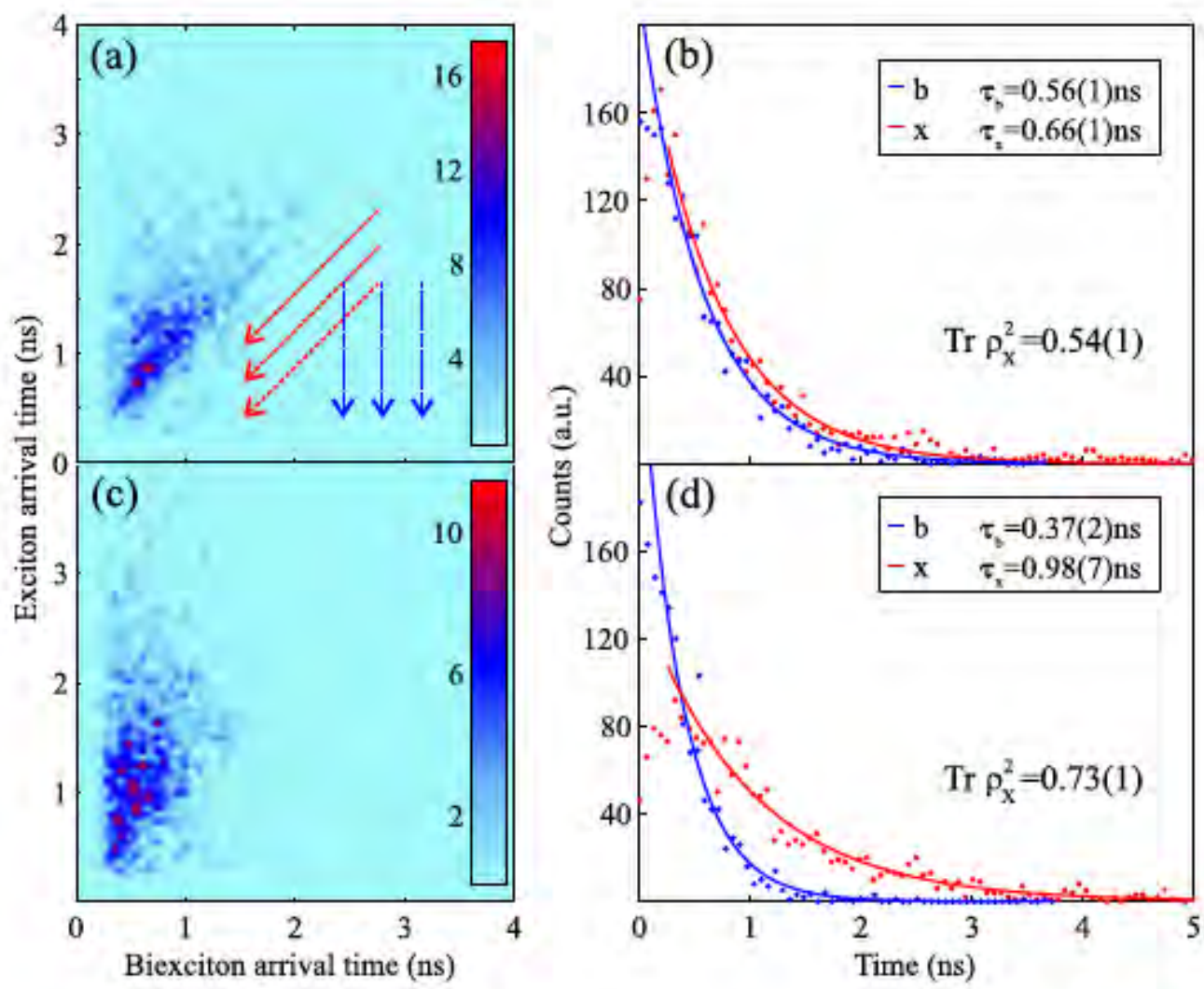


$$\psi(t_b, t_x) = 2\sqrt{\Gamma_b\Gamma_x}e^{-\Gamma_b t_b}\Theta(t_b)e^{-\Gamma_x(t_x-t_b)}\Theta(t_x - t_b)$$

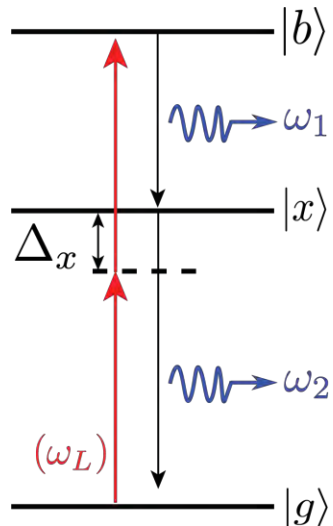
$$\rho_x = \text{Tr}_b(\psi^*\psi)$$

$$\text{Tr}(\rho_x^2) = \frac{\Gamma_b}{\Gamma_b + \Gamma_x}$$

Cascade correlations



Two – photon interference and cascade decay

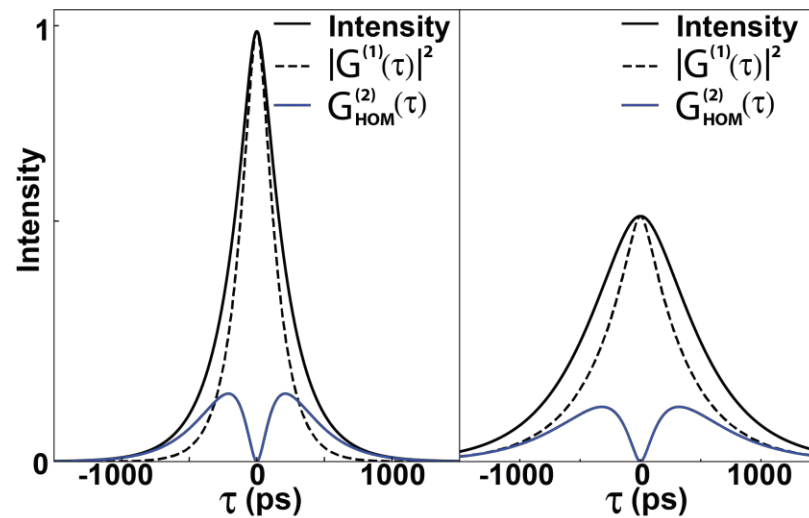
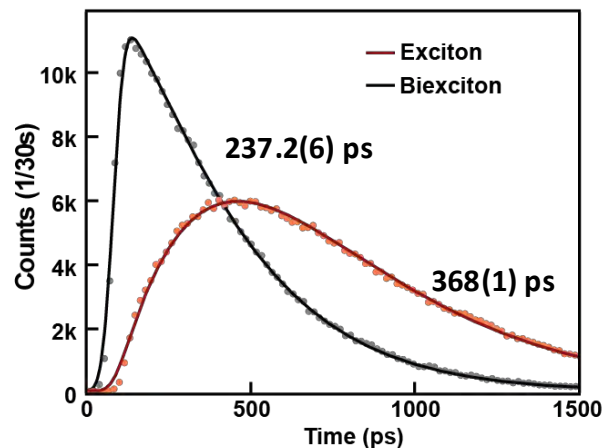


$$H_s = \sum_{j=1}^2 \left\{ \omega_j \xi_j^\dagger \xi_j + g \left[(\sigma_{xb} + \sigma_{gx}) \xi_j^\dagger + \text{h.c.} \right] \right\}$$

sensor method

$$\mathcal{L}_j \rho = \frac{\kappa_j}{2} \left(2 \xi_j \rho \xi_j^\dagger - \xi_j^\dagger \xi_j \rho - \rho \xi_j^\dagger \xi_j \right)$$

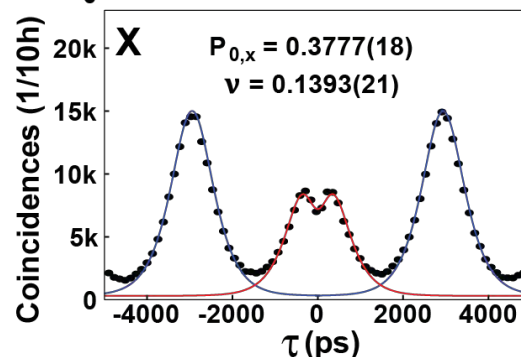
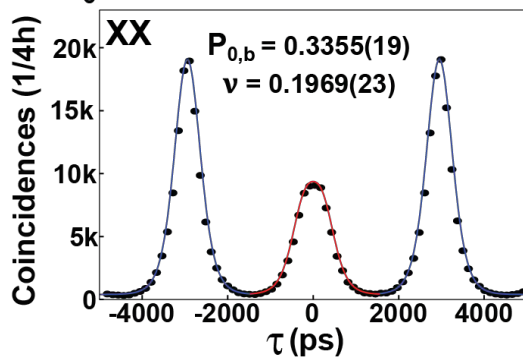
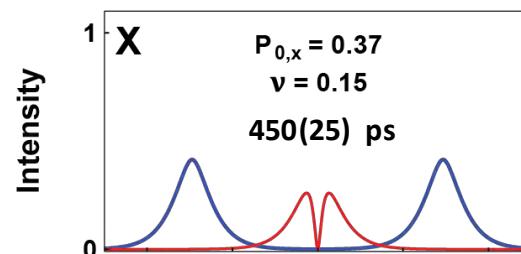
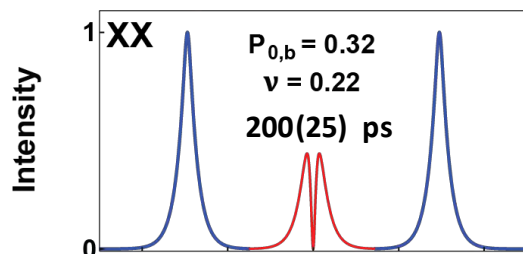
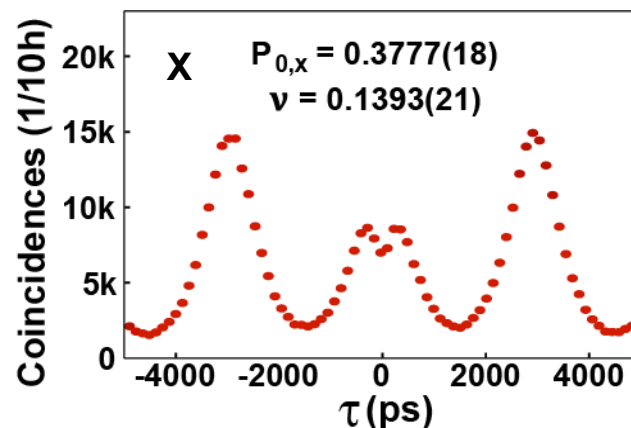
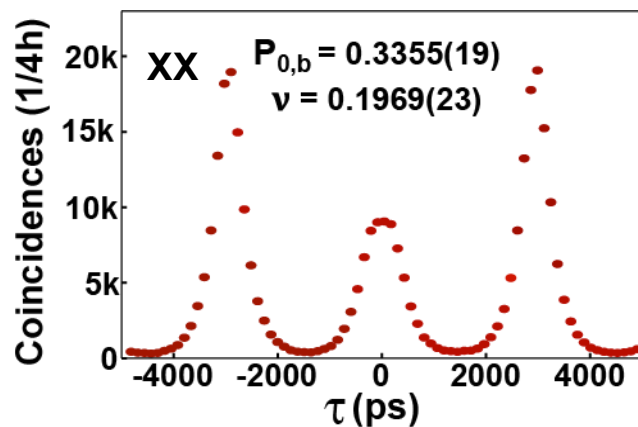
additional Lindblad terms



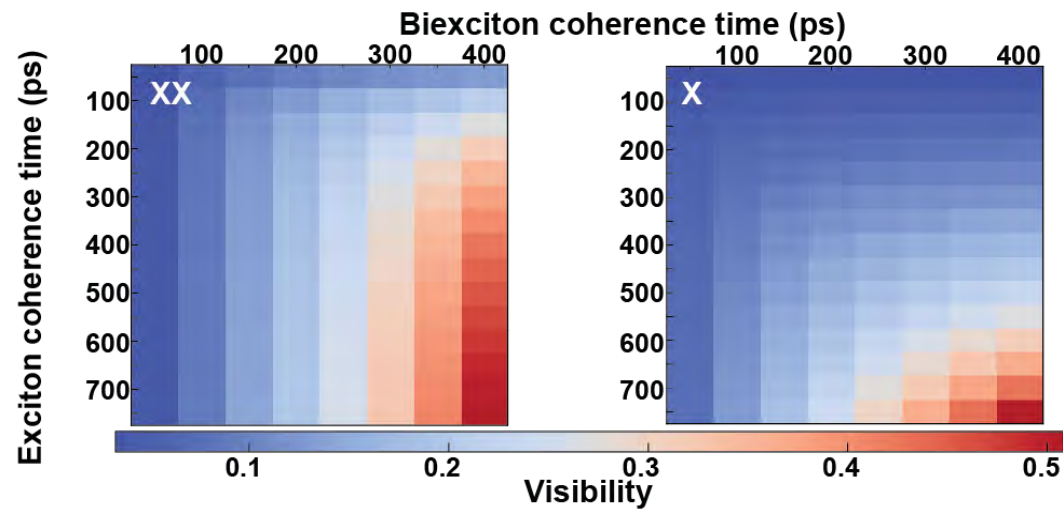
$$P_0 = 0.15$$

$$\text{visibility} = v = 0.54$$

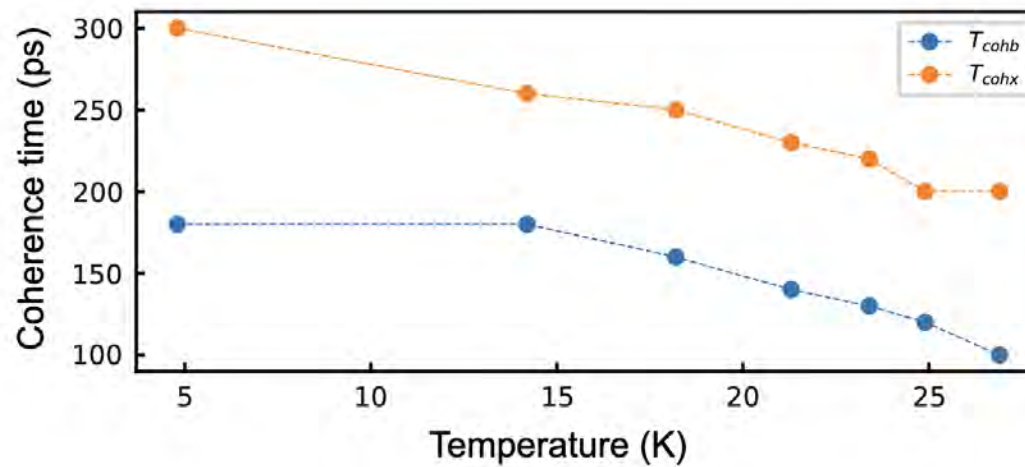
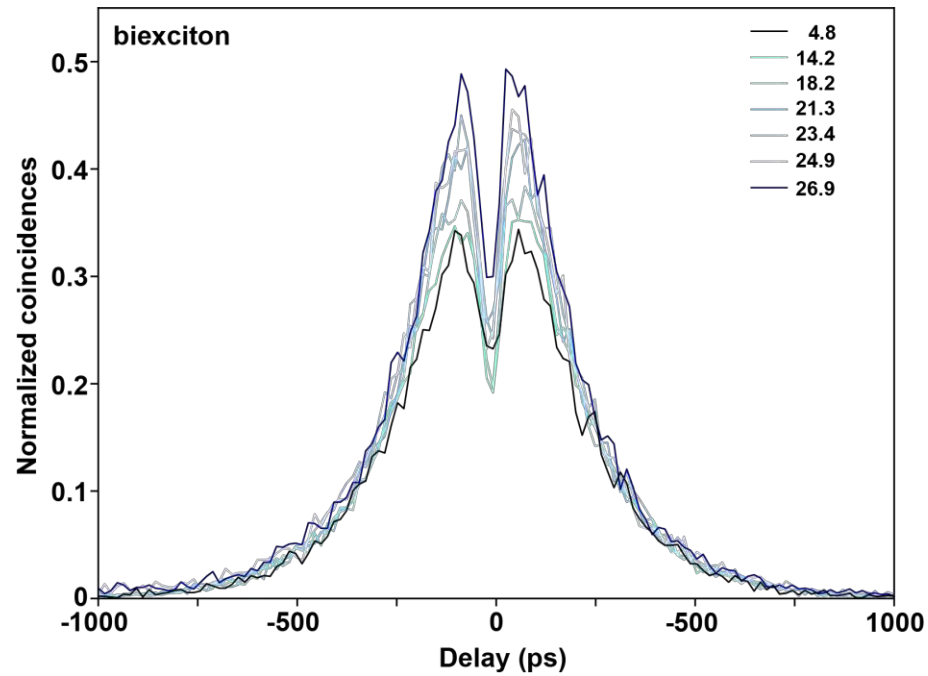
Two – photon interference and cascade decay



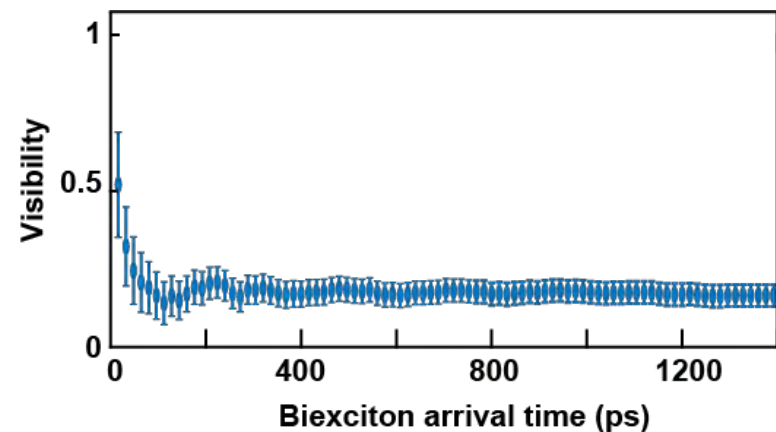
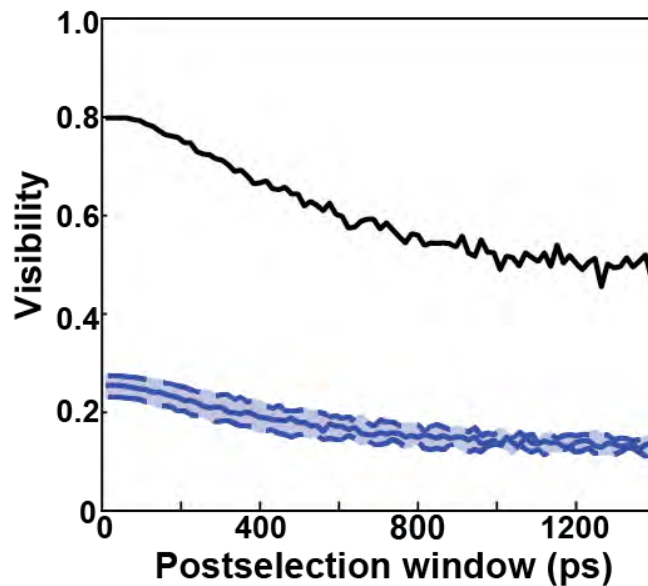
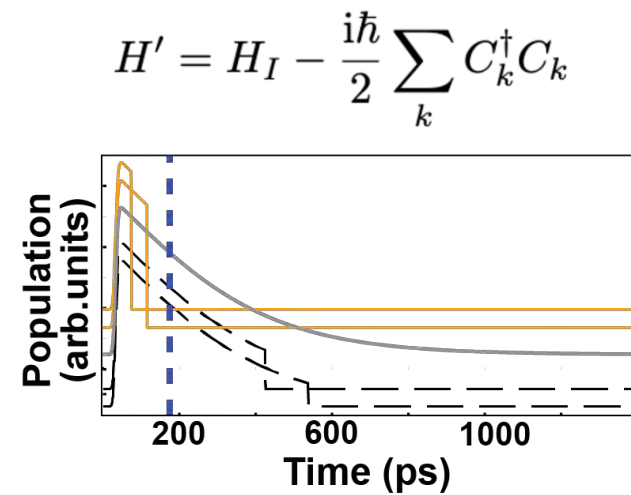
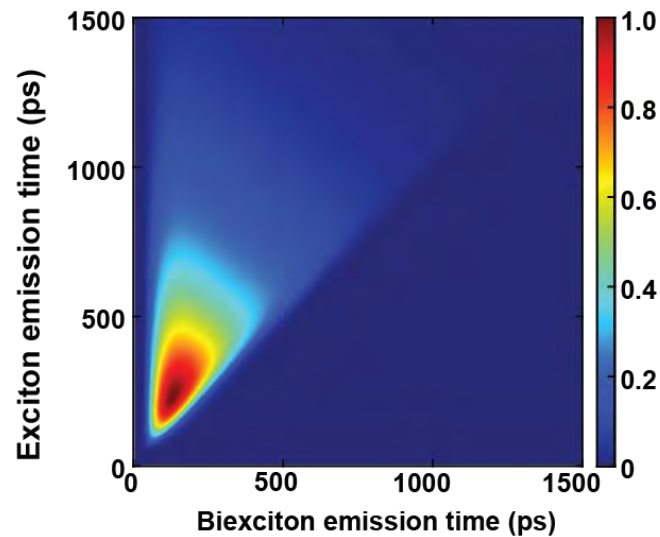
Two – photon interference and cascade decay



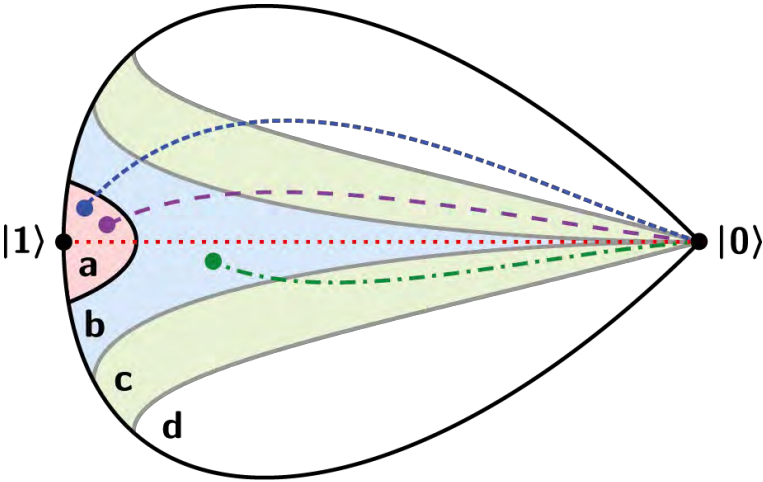
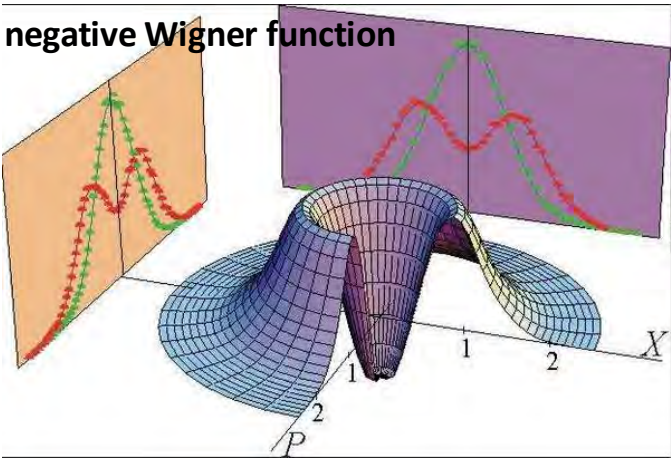
Two – photon interference and cascade decay



Two – photon interference and postselection



Losses resistant certification of quantum non-Gaussian states



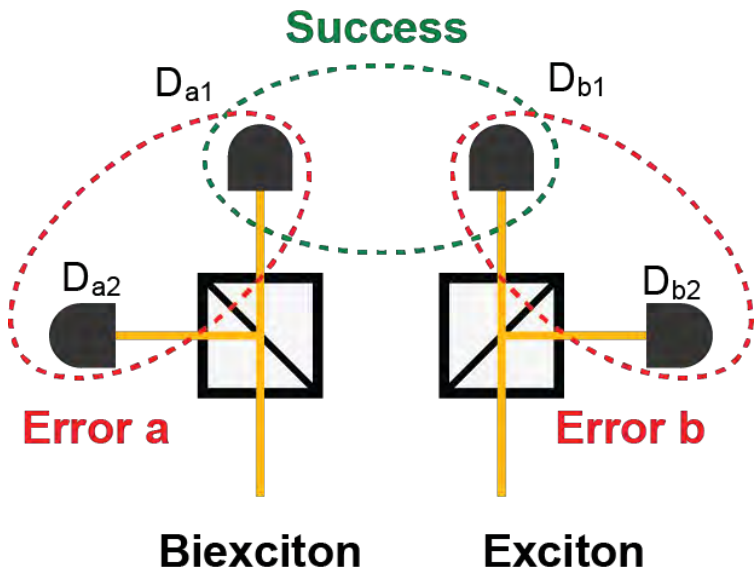
- a) negative Wigner function
- b) quantum non-Gaussian state
- c) non-classical state
- d) any other

photonic quantum states are subject to losses

I. Straka et al Phys. Rev. Lett. 113, 223603 (2014)

$$P_{1,\eta}^3 \gtrsim \eta / [4(2 - \eta)] P_{2,\eta}$$

η = the transmission of the lossy channel



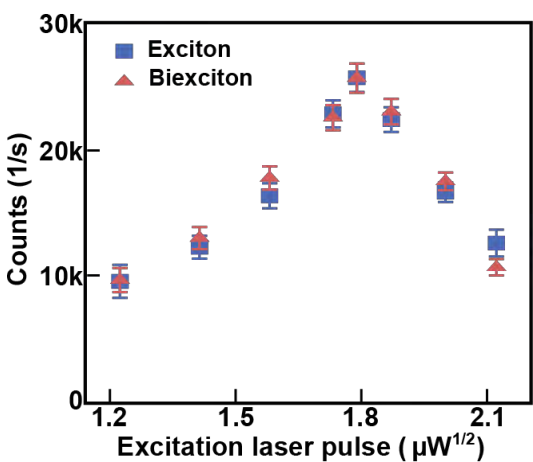
Two mayor challenges:

- a) accurate estimation of probabilities
- b) accurate estimation of the loss

$$P_{s,\eta} = C_s / C_0$$

$$P_{e,\eta} = (C_{e,a} + C_{e,b}) / 2C_0$$

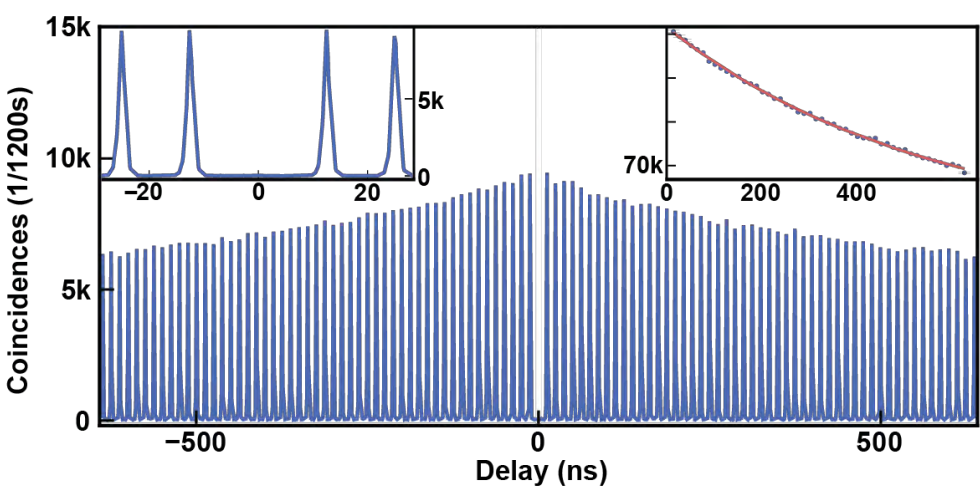
Losses resistant certification of quantum non-Gaussian states



$$P_{s,\eta} = C_s / C_0$$

$$C_0 = 11.32(12) \text{ MHz}$$

- a) blinking rate 0.56.6(6)
- b) excitation rate $\pi/2$
- c) polarization filtering 0.50

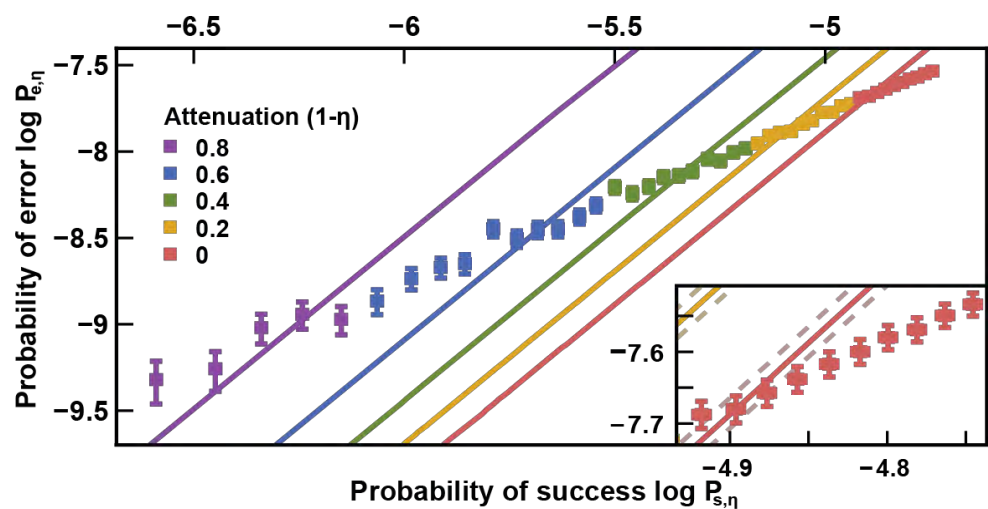


$$P_{e,\eta} = (C_{e,a} + C_{e,b})/2C_0$$

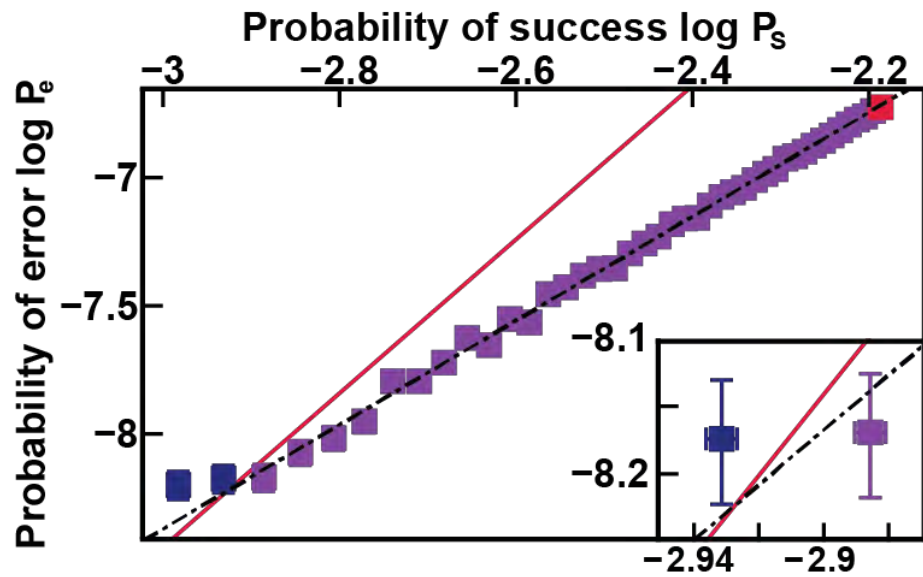
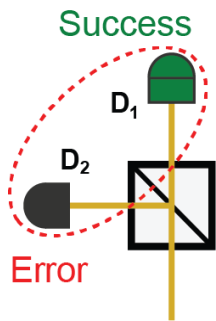
356(18)+430(21)

$$P_{s,\eta} = 1.797 \pm 0.020 \cdot 10^{-5}$$

$$P_{e,\eta} = 2.93 \pm 0.11 \cdot 10^{-8}$$



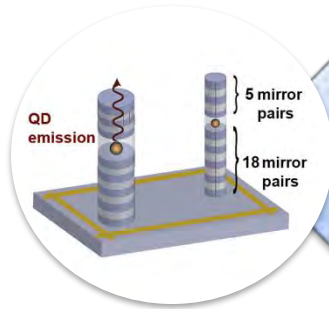
Attenuation ($1 - \eta$)	non-Gaussian depth (dB)
0	0.764 ± 0.039
0.2	0.740 ± 0.035
0.4	0.710 ± 0.033
0.6	0.667 ± 0.035
0.8	0.595 ± 0.049



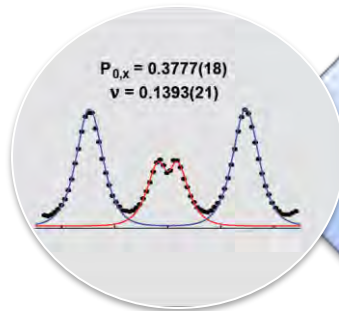
$7.41 \pm 0.11 \text{ dB}$

critierion is extremely resilient to losses

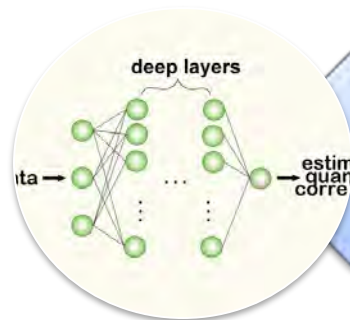
Quantum sources: efficiency, characterization, and entanglement generation



Novel sources of quantum light
Entanglement generation and efficiency engineering



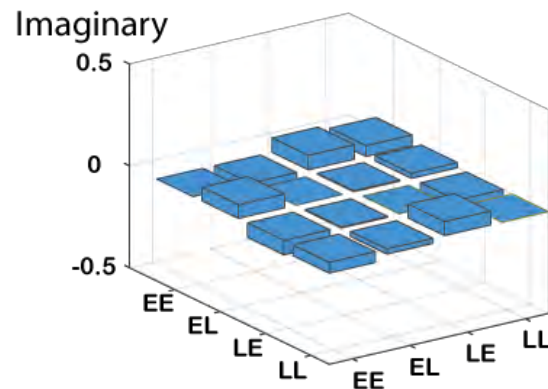
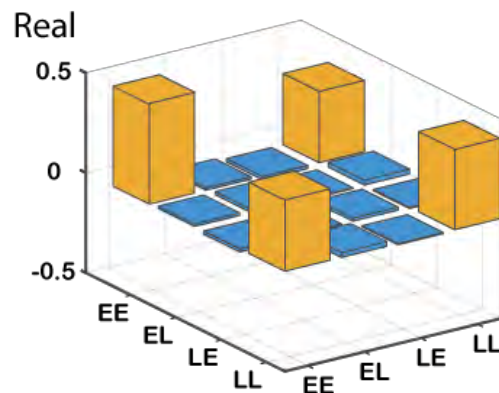
Intrinsic correlations
and two-photon interference and non-Gaussianity



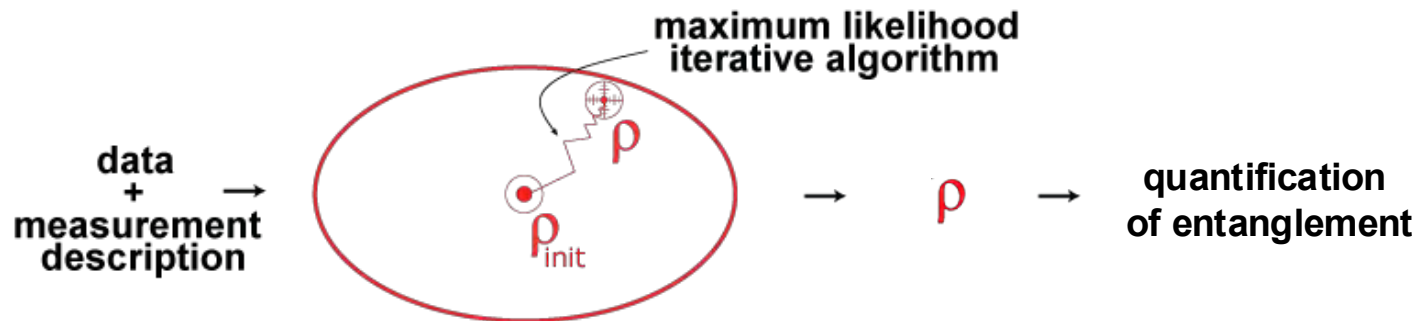
Machine learning for quantum technologies
Entanglement quantification

Entanglement quantification

- **direct measurement by interference of identical copies of the state**
P. Horodecki, Phys. Rev. Lett. 910, 167901 (2003).
- **quantum state tomography**
M. Paris, J. Rehacek, Quantum State Estimation (Springer-Verlag, 2004).
- **quantum state tomography with a priori information**
D. Gross, et al. Phys. Rev. Lett. 105, 150401 (2010).
- **shadow tomography**
S. Aaronson in STOC 2018: Proceedings of the 50th Annual ACM SIGACT Symposium on Theory of Computing (Association for Computing Machinery, 2018), pp. 325-388
- **entanglement witnessing**
P. Horodecki, A. Ekert, Phys. Rev. Lett. 89, 127902 (2002).



Entanglement quantification



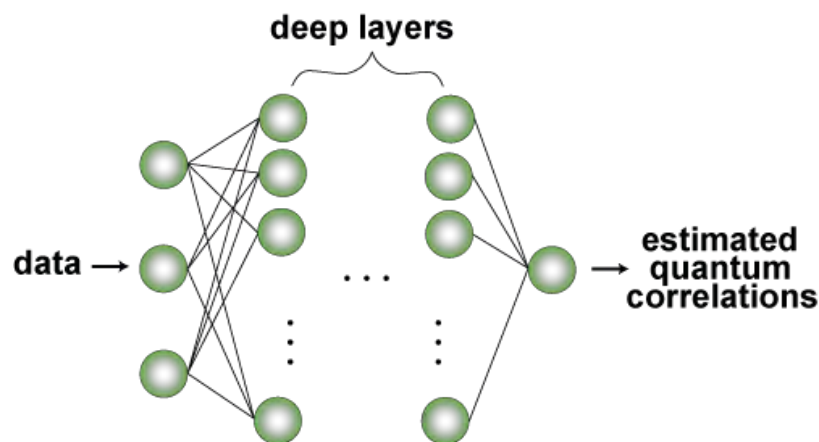
- demands the complete set of measurements (or assumptions about the state)
- inherently not scalable (example: photonic qubit 6^n , n =number of qubits)
- one needs to reconstruct ρ before entanglement can be quantified
- accuracy significantly decreased if an incomplete measurement is used

Examples of entanglement quantifiers:

- concurrence
- negativity
- entanglement of formation
- mutual information

Entanglement quantification

- trained using simulated data
- incomplete set of measurements
- quantify the quantum correlations via concurrence (2 qubits) and mutual information (more qubits) directly without need to know the state

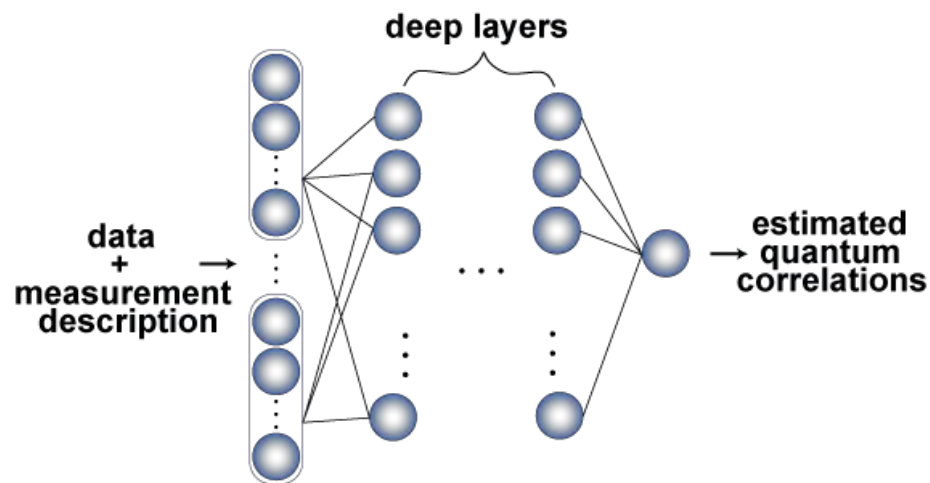


measurement specific



Entanglement quantification

- trained using simulated data
- incomplete set of measurements
- quantify the quantum correlations via concurrence (2 qubits) and mutual information (more qubits) directly without need to know the state

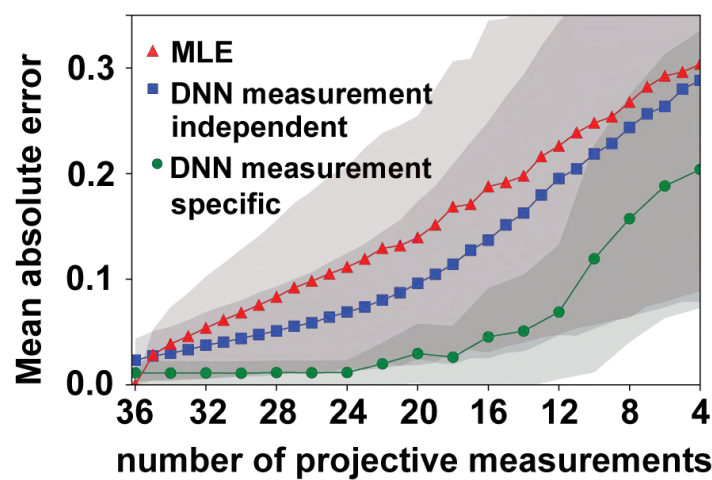


measurement independent

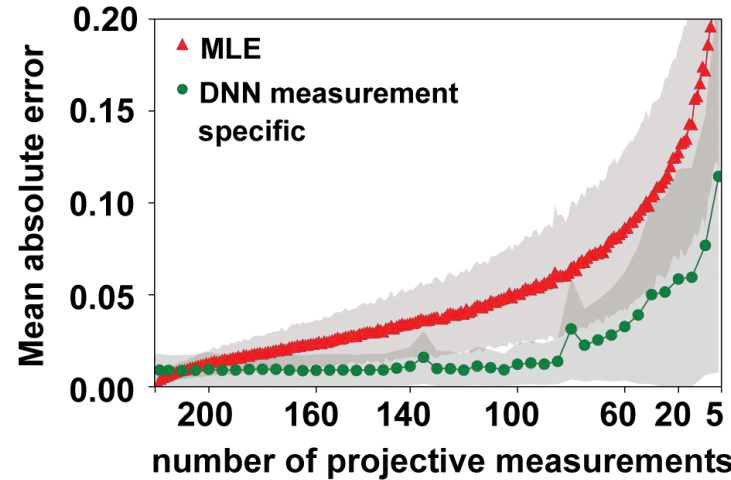


Entanglement quantification

2-qubit concurrence estimation using incomplete measurements



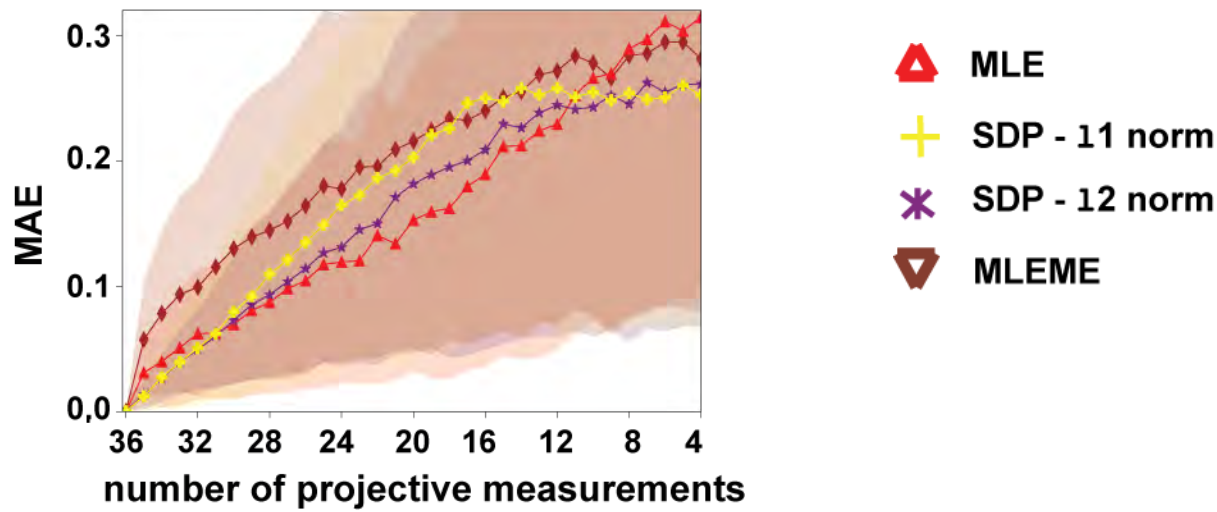
3-qubit mutual information estimation using incomplete measurements



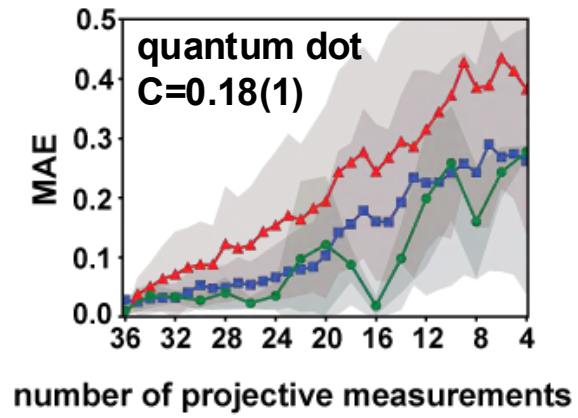
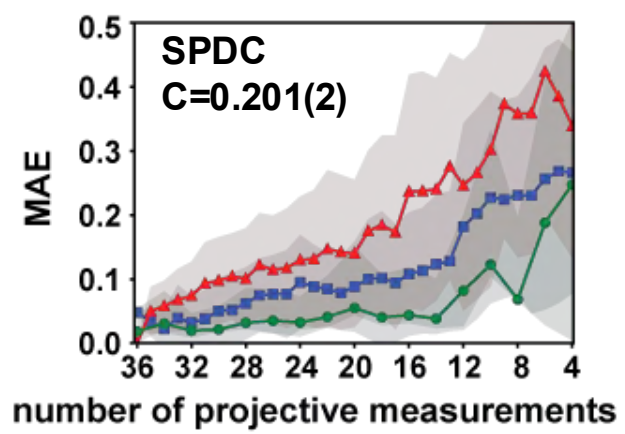
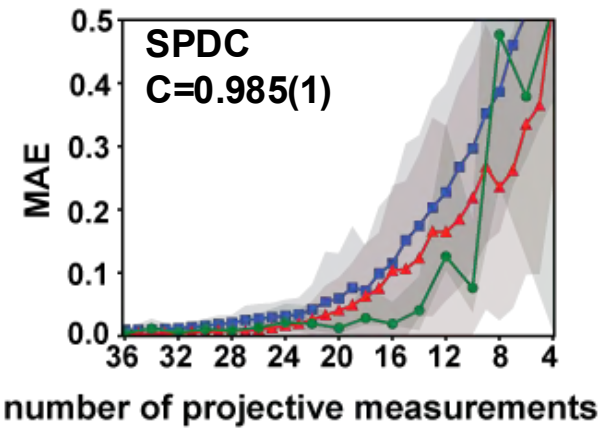
number of qubits	MAE		ratio of MLE and DNN MAEs
	MLE	DNN	
2	0.20 ± 0.16	0.09 ± 0.09	2.2
3	0.068 ± 0.055	0.023 ± 0.020	3.0
4	0.019 ± 0.014	0.005 ± 0.001	3.8
5	0.039 ± 0.032	0.009 ± 0.001	4.3

Entanglement quantification

number of qubits	MAE		ratio of MLE and DNN MAEs
	MLE	DNN	
2	0.20 ± 0.16	0.09 ± 0.09	2.2
3	0.068 ± 0.055	0.023 ± 0.020	3.0
4	0.019 ± 0.014	0.005 ± 0.001	3.8
5	0.039 ± 0.032	0.009 ± 0.001	4.3



Entanglement quantification



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